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**TRANSITION ON TURBINE BLADES AND
CASCADES AT LOW REYNOLDS
NUMBERS**

Richard B. Rivir

June 17-20, 1996

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Transition on Turbine Blades and Cascades at Low Reynolds Numbers

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Abstract

Unpredicted losses in the low pressure turbine during operation at high altitudes has stimulated current interest in transition, and separation at low Reynolds numbers. In the turbine, free stream turbulence levels or unsteadiness resulting from vane wakes, passage vortices, and end wall horseshoe vortices exceeds the unsteadiness levels associated with a fully turbulent boundary layer. Transition and transition length are found to be a function of both turbulence intensity and length scale although there are no empirical relationships to be found in the literature which include both. An experimental and computation effort was undertaken to investigate the effect of turbulence intensity, and turbulence length scale on transition location, and transition length in a Langston turbine cascade for solidities of 1.075 and 0.84 at Reynolds numbers of 50K to 2000K. Experimental observations of transition at turbulence levels of 1 and 10% for three integral turbulence scales indicate a relative lack of sensitivity to turbulence level and scale for the momentum thickness transition location, but a sensitivity to both for transition length.

Nomenclature

Bx	x projected turbine blade chord (m)
C	turbine blade chord (m)
c_μ	Turbulent coefficient of viscosity
K	acceleration parameter $(U^2/\nu) \partial U / \partial x$ ($1/s^2$)
p	turbine blade pitch (m)
s	surface distance on turbine blade (m)

Re_θ	Reynolds number based on momentum thickness
$Re_{\theta s}$	Reynolds number based on momentum thickness at separation
$Re_{l_{tr}}$	Reynolds number based on transition length
$Re_{s_{tr}}$	Reynolds number based on a transition after separation
t'	rms component of temperature ($^\circ/s$)
Tu	turbulence intensity (u'/U)
u'	rms component of x velocity (m/s)
U	x component of velocity (m/s)
v'	rms component of y velocity (m/s)
Λ_I	Integral scale of turbulence (m)
λ_μ	micro scale of turbulence (m)
λ_θ	acceleration parameter $(-\theta^2/\nu) \partial U / \partial x$
θ	momentum thickness (m)

Introduction

The commonly held physical picture of the transition process is illustrated schematically in Figure 1. Two D Tollmien Schlichting waves are amplified, breaking down into Emmons spots which propagate as a wedge with a following quiet wedge region until the boundary layer has become fully turbulent. Turbine transitions normally will bypass the Tollmien Schlichting part of the process and break down directly as a result of the high levels of unsteadiness present. A laminar separation with transition in the separation bubble, as is also illustrated in Figure 1, is not an uncommon mode of turbine transition since turbines must operate over a wide range of conditions which include large

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changes in angles of incidence, Re , and inlet distortions.

Mayle's 1991 review paper provided the most recent comprehensive look at the transition problems in turbine engines. There has been no shortage of transition papers as well since Mayle's work. Walker, 1993 and Roshoko, 1994 have published subsequent surveys. Additional surveys can be found in *Euromech 327*, *Ercoftac Bulletin March 1995*, *AGARD CP-551 Application of Direct and Large Eddy Simulation to Transition and Turbulence 1994*, and the *Syracuse University Minnowbrook Work Shop on End Stage Boundary Layer Transition*, 1993.

Mayle's paper provided a compilation of useful empirical relationships and data for Tu levels below 8%. Bypass transition is the primary mechanism of interest in turbine related flows due to the high levels of unsteadiness - although all transition mechanisms can exist at different times at the same location on a blade. According to Mayle deficiencies that existed in 1991 included a lack of $u'v'$ and $v't'$ measurements, virtually no measured turbulence length scales at transition, and scarce transition measurements in accelerating and decelerating flows.

Since 1991, Zhou and Wang 1993 measured $u'v'$ and $v't'$ in a zero pressure gradient and in a favorable pressure gradient, transitioning flat plate flow with grid generated turbulence up to 6.4%. They observed large changes in the spot formation rate with the acceleration parameter K . The turbulent spot formation decreased by an order of magnitude at the higher turbulence levels with a doubling of the acceleration parameter.

Volino and Simon, 1995 provided detailed measurements of transitional boundary layers on concave surfaces with Tu up to 8%. The production of wall disturbances began transition when K was less than 2×10^{-6} . For strong acceleration, $K > 3 \times 10^{-6}$, they found that the intermittency became nearly constant and transition was inhibited. However even at the highest value of their acceleration parameter, $K = 9 \times 10^{-6}$ and $Tu = 8\%$, there still was an extended transitional region which was dominated by the free stream scales with fluctuations in heat transfer and skin friction between fully turbulent and laminar. Under these conditions the transition became intermittent, with Tu dropping from 8% to 1.6% through the acceleration region. As Tu dropped to 1.6% the favorable acceleration took over dominating and suppressing any tendency to transition.

Simon, 1995 gave two empirical relationships for the variation of transition length with momentum thickness Re and suggested, as did Mayle, that

additional experimental data is needed. Walker, 1993, also addressed transition length suggesting that K is an inappropriate parameter, and that if one chooses $\lambda_\theta = (\theta^2/\nu)dU/dx$ as the acceleration parameter, the effect of acceleration may be included in the transition length relationship.

Laminar separation with a subsequent transition, as illustrated in Figure 1, can and does occur on turbine blades. Walker suggests $Re_{est} = 700Re_{\theta\theta}^{0.7}$ in laminar separation bubbles. Measurements of transition in separation bubbles are difficult and very scarce. There remain many uncertainties in the recovery region of separation bubbles as to whether transition has been completed or not, as well as to exactly which parameters and characterizations are relevant for transition in laminar separated flows.

Since modern turbine blades have high aft loading transition location, transition length, and flow separation have a significant influence on their performance. C-17(F-117) engines as well as smaller engines with their associated smaller blades typically exhibit higher than predicted SFC during high altitude operation. The additional operational loss in SFC can amount to 0.8% over design calculations. The current inability to accurately predict the transition, separation, and reattachment at low Reynolds numbers in turbines is associated with the high levels of turbulence and unsteadiness of the flow. A low pressure turbine typically operates at a chord Reynolds number of 10^6 at take off. The chord Reynolds number falls to 10^5 at altitude in a number of engines. Sharma, 1994, reported a near doubling of the measured loss coefficient, as illustrated in Figure 2, from cascade measurements, when the chord Reynolds number is reduced from 300K to 50K.

In our work on low pressure, low Reynolds number turbine flows we have a few new measurements of transition, transition length and turbulence scales to add to the above picture for the free stream turbulence levels of 1 and 10%. The experimental measurements have been performed in a Langston cascade with two pitch to chord ratios and three turbulence scales. Computations using the Allision Blade Vane Interaction program, a 2 D Navier-Stokes solver, for two pitch to chord ratios and six chord Reynolds numbers have also been carried out and will be compared to the experimental measurements.

Low Reynolds Number Cascade

A Combined experimental and computational study was conducted to investigate transition over the suction surface of a low Reynolds number turbine cascade to

determine how it is affected by freestream turbulence intensity, freestream turbulence scale, and solidity (C/p). The Langston cascade, Langston et al., 1977, was chosen as the geometry for investigation since it is a well documented geometry at higher Reynolds numbers, while still fairly representative of current low pressure turbine geometries. Two similar experimental cascades were used, one at the Air Force Academy and one at UC Davis, the documentation of both will be found in Baughn et al., 1995. The nominal cascade chord is 17.1cm and the aspect ratio 3.9. The investigation spanned a range of solidities of 0.084 to 1.075, turbulence levels from 0.5% to 10%, and integral turbulence scales from .0054m to 0.0704m. Computations for two of the experimental solidity ratios ($C/p=0.84$ and 1.075) have been carried out at six chord Reynolds numbers (50K, 100K, 200K, 441K, 1,000K, and 2,000K).

Computational Results

The computational code used for the numerical simulation of the steady Navier-Stokes equations was the VBI code developed by the Allison engine company, Rao et al., 1994, under U.S. Air Force contract. The steady state solution of the code is based on a five step Runge Kutta relaxation method that incorporates residual smoothing to accelerate convergence to the final solution. The code implements a Baldwin-Lomax, 1978, two-layer algebraic turbulence model and the Baldwin-Lomax transition point model. There is no transition length associated with this turbulence model, transition occurs at the fixed recommended value of the turbulent viscosity coefficient, $c_\mu=14$, which corresponds to $Re_\delta=300-419$. The grid used in this code is an overlaid combination of a rectangular H grid and a body fitted hyperbolic O grid. The rectangular grid is used to resolve the free stream flow and the O grid is used to resolve the regions of high shear associated with the boundary layer. Small values of y^+ have been employed in the calculation for the O grid spacing, with the first grid point at a y^+ of 1 or less.

The computational results presented in Figures 3 through 5 demonstrate the effect of chord Re on the computed boundary layer characteristics on the blade suction surface for two solidities. Figure 3 and 4 show typical Re_δ variations over the blade suction surface at a chord Re of 50K for the two solidities of 0.84 and 1.075 respectively. In the first case ($C/p=0.84$) the suction surface boundary layer undergoes transition at the computed $Re_\delta=310$ followed by separation and then laminar reattachment. When the solidity is increased

to, $C/p=1.075$ (Figure 4), the boundary layer over the suction surface undergoes laminar separation (as illustrated schematically in Figure 1) before transition at $Re_\delta=347$ and turbulent reattachment near the trailing edge. The computed transition locations for the two chord to solidities at six Reynolds numbers ranging from 50K to 2000K is presented in Figure 5. The results indicate that in general the transition location moves forward as Reynolds number increases. The transition location occurs earlier for the low solidity case, however these flows were found to suffer severe flow separations. Depending on the solidity, the entire suction surface boundary layer becomes turbulent above a chord Re of 1000K for $C/p=1.075$, and above 100K for $C/p=0.84$. The complete results including separation and reattachment calculations for these flows can be found in Rivir et al., 1996. These results will next be compared with the experimental low (1%) freestream turbulence case.

Experimental Measurements of Low Reynolds Number Transition

Experimental measurements for transition location and transition length were obtained at low Reynolds numbers (64K-144K) in the Langston Cascade for solidities ranging from 0.084 to 1.075. The location of the transition, separation, and reattachment points were determined by a narrow band liquid crystal which was applied to a vapor deposited gold heated film on the surface of the cascade airfoil. Turbulence ($Tu=0.5$, 1, and 10%) was generated by square mesh grids which were nominally located > 25 mesh distances upstream, so that turbulence was in the final period of decay and slowly changing with x . The integral scale of turbulence (0.005m to 0.0704m) was measured by autocorrelation of the hot wire signal along with Taylor's Hypothesis. The micro scale was obtained from $1/\lambda_\mu = -1/U(\partial^2 R(T)/\partial T^2)$ applied to the autocorrelation function $R(T)$ of the hot wire's signal. Three square mesh turbulence grids were employed, all of which generate 10% freestream levels of Tu . The grid generated turbulence scale characteristics investigated are tabulated in Table 1.

Also presented on Figure 5 are the experimentally measured transition locations at a chord Re of 67K ($C/p=1.075$) and 110K ($C/p=0.84$) at $Tu=1\%$. The agreement with the computational results for the two solidities is excellent. The $C/p=0.84$ experimental case was observed to relaminarize and then transition again at a s/Bx of 0.93.

Effect of Turbulence Intensity

Transition Location $Re_{\theta t}$

Figure 6 shows Mayle's empirical relationship for $Re_{\theta t}$ dependence on Tu with the original data he used which indicates increased $Re_{\theta t}$ with increasing Tu scale. Figure 6 also includes three additional sets of data that were not included in Mayle's paper. The first set represents Zhou and Wang's 1993 measurements in zero and favorable pressure gradient transitioning flat plate flows. These results were obtained at grid generated turbulence levels of 0.5 to 6.4% and turbulence scales of 1.8 to 2.8cm, showing excellent agreement with Mayle's correlation. Zhou and Wang also added acceleration with only a small resulting increase (110 to 130) in $Re_{\theta t}$. Mayle's value at 2.2% Tu for $K=0.75 \times 10^{-6}$, was 244. The second and third sets correspond to experimental measurements in the Langston cascade and Dring's rotating Langston cascade. The second set represents the experimental results from Baughn et al., 1995 which were obtained at $Tu=1\%$ and 10% in the Langston cascade. In these experiments surface heat transfer measurements were used to determine the transition locations, s/Bx . The computational results from Rivir et al., 1996 were then used to deduce the value of $Re_{\theta t}$ based upon the measured experimental transition locations. The $Tu=1\%$ points correspond well to the empirical relationship while the $Tu=10\%$ points show a much larger value (5x) for $Re_{\theta t}$ than the empirical relationship. The third data point shown on Figure 6 is from Dring et al., 1986 rotating low Re Langston cascade (see Table 1). Again the empirical prediction under predicts the $Re_{\theta t}$ by a factor of two. The rotating and 10% cascade data show the general trend with scale but are not accurately captured by the empirical models.

Transition Length

The experimentally measured surface heat transfer data in the low Re Langston cascade are presented in Figure 7 for turbulence levels of 1% and 10% . Figure 7 illustrates the effect of turbulence intensity on the apparent length of transition, comparing the $Tu=1\%$ and the $Tu=10\%$ data, at nominally the same Re , we see transition moves forward with increasing Tu and the length of the transition increases. Figure 8 presents two empirical relationships for the $Re_{\theta t}$ dependence from Simon. The two correlations are $Re_{\theta t} = 124 \cdot Re_{\theta tr}^{3/2}$ for a zero pressure gradient, and $Re_{\theta t} = 344 \cdot Re_{\theta tr}^{3/2}$ for a weak pressure gradient ($K=0.75 \times 10^{-6}$). Lacking an exact measurement of velocity at transition the range of velocities was

determined based upon the cascade entrance and exit velocities. The range of transition lengths from the experimental measurements indicate transition length Reynolds numbers of 20K to 83K. Using the calculated values of $Re_{\theta t}$, as explained in the previous section, the cascade experiments at low Reynolds numbers fall near the zero pressure gradient relation, $124 \cdot Re_{\theta tr}^{3/2}$. Although we have not yet measured $Re_{\theta t}$ directly it is clearly much larger for the cascade from comparison of s/Bx at transition in Table 1 than obtained in Dring's rotating test of the Langston cascade.

Combining Mayle's $Re_{\theta t} = 400 Tu^{-5/8}$ with Simon's above relationships gives Figure 9 for the two Simons curves, the third curve is a similar relation from Mayle with $\theta_e = \theta_t$. Both the high turbulence ($Tu=10\%$) data for the cascade as well as Dring's 1986 low Re rotating data fall well below Simon's upper curve which is for small acceleration ($K=0.75 \times 10^{-6}$). The acceleration at transition for the Langston cascade is calculated to be on the order of 3×10^{-5} , at $Re=50K$, an order of magnitude higher. The low Re data therefore should have fallen above the top curve if the top curve was also applicable for strong accelerations. Here one should heed Volino and Simon's observation that typical turbine blade accelerations virtually shut off boundary layer turbulence generation. The 1% Tu case is also shown on Figure 9 and is 1 to 2 orders of magnitude below Mayle's and Simon's correlations respectively. This would indicate that this relationship with Tu may also be much flatter than current empirical models predict. A common assumption used is that the velocity fluctuations are frozen through the blade passage so turbulence is expected to change along the blade suction and pressure surfaces as the freestream velocity varies and like wise the turbulence at transition will be significantly less than at the cascade entrance. Revised empirical relationships are required to accurately describe the low pressure, low Re turbine flows.

Effect of Turbulence Scale

The characteristics of the three turbulence grids employed in the low Re turbine cascade experiment are listed in Table 1 along with the corresponding locations of transition and transition lengths. The experimentally measured location of transition by Sharp and Harris, 1996 is shown in Figure 10 for two grids and the clean tunnel ($\Lambda_1=0.0704m$, $\Lambda_2=0.0132m$, $\Lambda_3=0.0054m$) at chord Re 's of 76.7K and 79.9K. The transition location s/Bx moved forward, as turbulence increased from 0.5% to 10% . The forward movement

in s/Bx is in this case small. Both grids produced 10% turbulence intensities at the cascade face and both resulted in transition at the same value of s/Bx . The transition length was significantly altered with the larger scale increasing the length by 30% as seen in Figure 10.

It has not been established whether the transition is complete at the trailing edge of our Langston cascade blade. The electrodes for the gold foil surface are located at the trailing edge creating a small discontinuity in the heat flux per unit area which may be altering the trailing edge observations. The observed heat transfer level at the trailing edge is flattened and appears to be in between laminar and turbulent for the transitioning cases investigated. It remains to be determined with detailed velocity profiles whether the transition is complete at the trailing edge or still under development and unsteady. The resulting freestream Tu level and Tu scales should be documented during transition for accelerating turbine cascade flows. These determinations would of course influence the interpretation of transition length, but even more important the state of the boundary layer in this flat region and its implication on losses.

Figure 11 presents the results for all three grids investigated relating the integral scale of turbulence to transition location and transition length. The location does not change significantly over the range of integral scales investigated. The length of transition does however increase slightly with an increase in scale. Dring's rotating data again is indicated for comparison and we see comparable transition lengths but a significantly forward transition location or $Re_{\delta t}$.

Summary

The Low Reynolds number computations in the Langston cascade show oscillating transition, separation and reattachments. The experimental cascade measurements indicate weak $Re_{\delta t}$ dependency on with turbulence intensity for the turbulence scales investigated. The calculations showed good agreement with the experiment for both C/p ratio of 1.075 and 0.84 for $Tu=1\%$. Both our experiments and our calculations show strong effects of the solidity on the transition length and the tendency towards laminar separation (with subsequent transition) at low solidities. Although we are still lacking detailed velocity profiles at transition for the Langston cascade, it would appear that the acceleration parameter K does not influence turbulence intensity's effect on transition length to the same degree observed in flat plate experiments. The effects of turbulence scale on

transition were also found to be modified in the cascade. At 10% freestream turbulence the $Re_{\delta t}$ and x location of transition was unaffected by turbulence scale. The transition length however increased by 30% when the turbulence scale increased decreased by 81%.

The comparison with the rotating Langston turbine indicates that $Re_{\delta t}$ is modified by rotation significantly while the transition length is unaffected. Turbulence scale effects in both cascades and rotating experiments appear to significantly alter the current empirical flat plate relationships.

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References

- "Application of Direct and Large Eddy Simulation to Transition and Turbulence", December 1994, AGARD-CP-551.
- "European Research Community On Flow Turbulence and Combustion" Bulletin, March 1995.
- Baldwin, B. S., and Lomax, H., 1978, "Thin-Layer Approximation and Algebraic Model for Separated Turbulent Flows," AIAA Paper 78-0257.
- Baughn, J. W., Butler, R. J., Byerley, A. R., and Rivir R. B., August 1995, "An Experimental Investigation of Heat Transfer, Transition and Separation On Turbine Blades at Low Reynolds Number and High Turbulence Intensity," 1995 ASME International Mechanical Engineering Congress and Exposition.
- Dring, R. P., Blair, M. F., and Joslyn, H. D., 1986, "The Effects of Inlet Turbulence and Rotor Stator Interactions on the Aerodynamic and Heat Transfer of a Large Scale Rotating Turbine Model, Volume 11-Heat Transfer Data Tabulation, 15% Axial Spacing," NASA CR 179467, UTRC-R86-956480-2.
- Langston, L. S., Nice, M. L., and Hopper, R. M., 1977, "Three Dimensional Flow within a Turbine Cascade Passage," *Journal for Engineering and Power*, Vol. 99, pp. 21-28.

- LaGraff, J.E., 1993, "Syracuse University Minnowbrook Workshop on End-Stage Boundary Layer Transition".
- Mayle, R.E., 1991, "The Role of Laminar-Turbulent Transition in Gas Turbine Engines", ASME paper 91-GT-282.
- Reshotko, E., 1994, "Boundary Layer Instability, Transition and Control", AIAA paper 94-0001.
- Sharma, O., P., Ni, R.H., and Tanrikut, S., 1994, Turbomachinery Design Using CFD. "Unsteady Flows in Turbines--Impact on Design Procedure", AGARD-LS-195, Paper No. 5.
- Sharp, J. and Harris, P., 1996, "Turbulent Heat Transfer Investigation: Turbulence Length Scales and Turbine Heat Transfer", United States Air Force Academy, Aeronautical Engineering 471 Report.
- Simon, F.F., 1994, "The Use of Transition Region Characteristics to Improve the Numerical Simulation of Heat Transfer in Bypass Transitional Flows", NASA TM 106445.
- Rao, K. V., Delaney, R. A., and Dunn M. G., "Vane-Blade Interaction in a Transonic Turbine, Part I Aerodynamics," May-June 1994, *Journal of Propulsion and Power*, Vol. 10 No. 3, pp. 305-311.
- Rivir, R., Sondergaard R., Dalhstrom M., and Ervin E., "Low Reynolds Number Turbine Blade Cascade Calculations," February 1996, ISROMAC-6 The 6th International Symposium on Transport Phenomena and Dynamics of Rotating Machinery, Honolulu, HA.
- Roberts, W.B., 1980, "Calculation of Laminar Separation Bubbles and their Effect on Airfoil Performance," AIAA Journal, Vol. 18 pp 25-31.
- Volino, R.J., and Simon, T.W., 1995, "Measurements in Transitional Boundary Layers Under High Free-Stream Turbulence and Strong Acceleration Conditions," NASA CR 198413.
- Walker, G.J., 1975, "Observations of Separated Laminar Flow on Axial Turbomachine Blading," AIAA Journal, Vol. 27, pp 595-602.
- Walker, G.J., 1993, "The Role of Laminar-Turbulent Transition in Gas Turbine Engines: A Discussion", ASME Journal of Turbomachinery, Vol. 115, pp 207-217.
- White F.M., 1974, *Viscous Fluid Flow*, McGraw-Hill, New York, NY.
- Zhou, D., and Wang, T., 1993, "Effects of Elevated Free-Stream Turbulence and Streamwise Acceleration on Flow and Thermal Structures in Transitional Boundary Layers", Final Report, Office of Naval Research, Grant No. N00014-89-J-3105.

Table 1 Grid, Turbulence Scale Characteristics

Re	Λ_I (m)	λ_μ (m)	Tu%	s/Bx_t	L_t/Bx	Reference
67K	0.006		0.5	0.25, 0.9	0.25	Baughn et al., 1995
76.7	0.0054		0.5	1.113	0.297	Sharp and Harris, 1966
79.9K	0.0132	0.005	10	0.964	0.297	Sharp and Harris, 1966
134K	0.0404	0.006	10	1.0	0.5	Baughn et al., 1995
76K	0.0704	0.008	10	0.983	0.537	Sharp and Harris, 1996
134K	0.0203	0.002	9.8	0.4	0.4	Dring et al., 1986

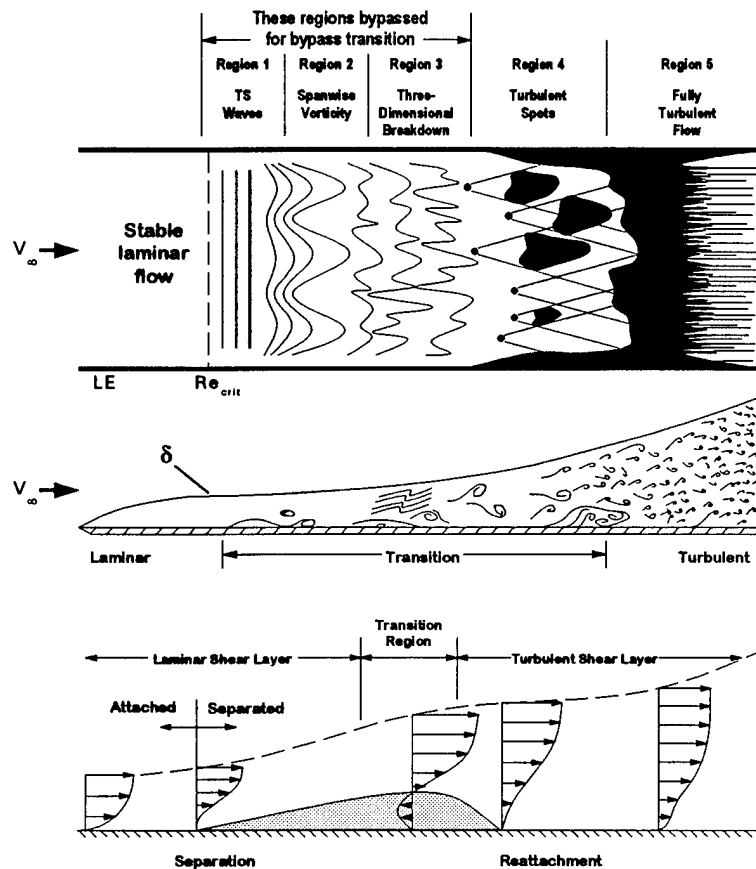


Figure 1. Schematics of the Transition Process / Schematic of Laminar Separation with Transition (White, 1974 / Walker, 1975, and Roberts, 1990)

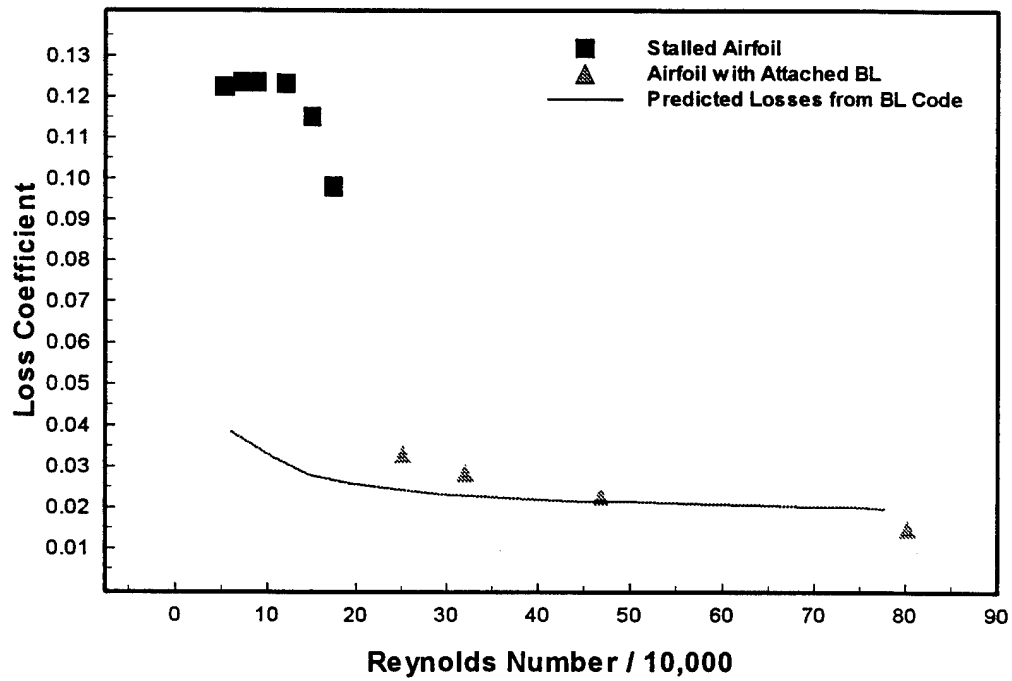


Figure 2. Cascade Losses at Low Reynolds Number (Sharma, 1994)

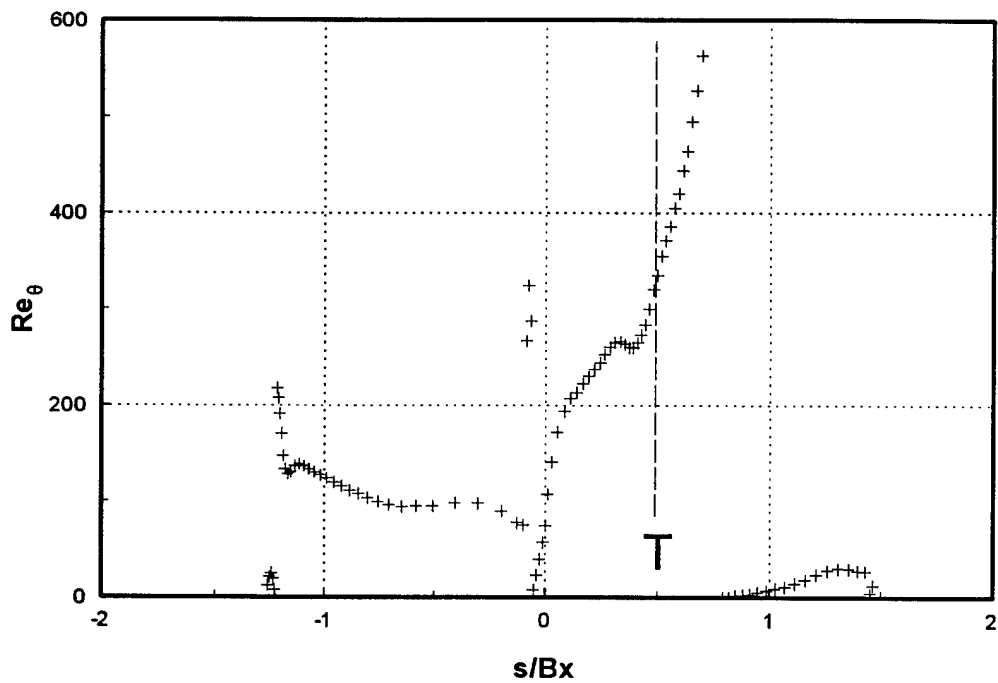


Figure 3. Momentum Thickness Reynolds Number at Transition for a Langston Cascade
Chord Reynolds Number of 50k, $C/p = 0.84$

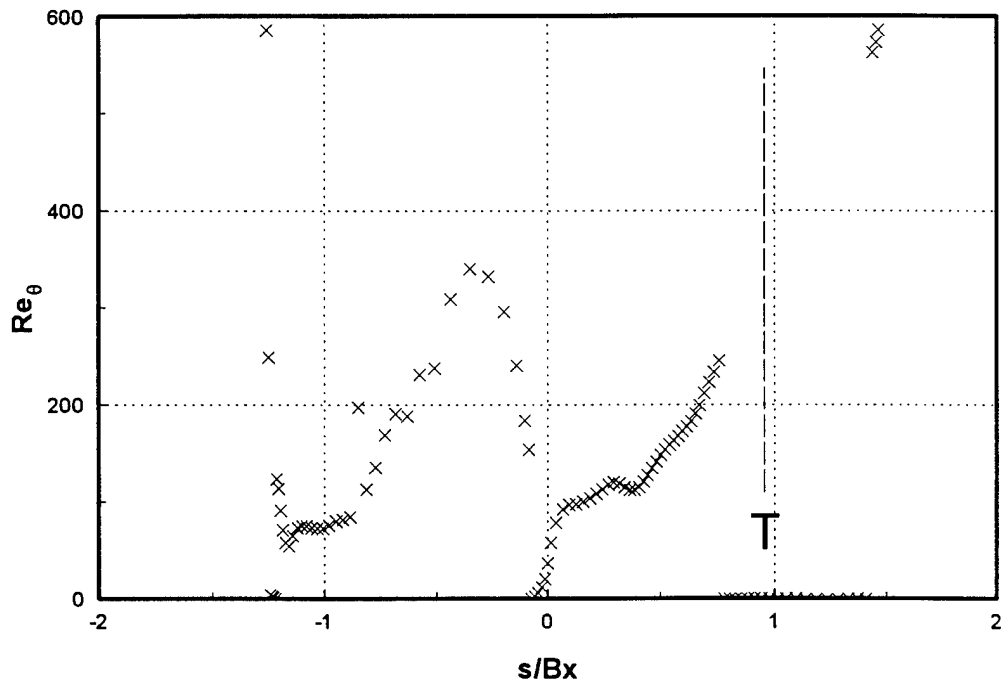


Figure 4. Momentum Thickness Reynolds Number at Transition for a Langston Cascade
Chord Reynolds Number of 50k, $C/p = 1.075$

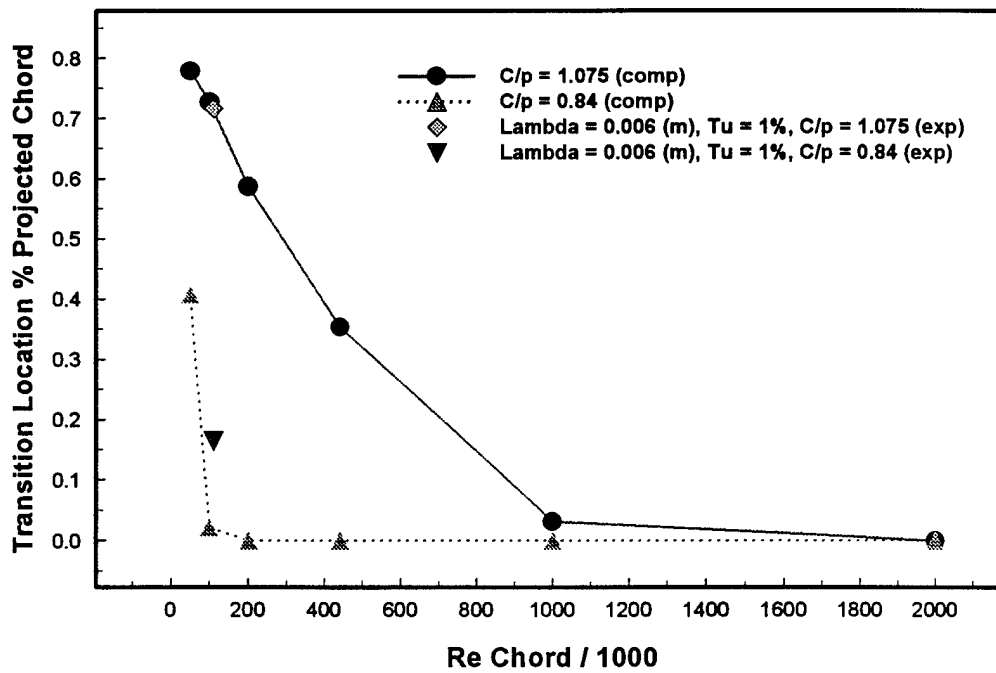


Figure 5. Transition Reynolds Number Dependence in % Projected Chord

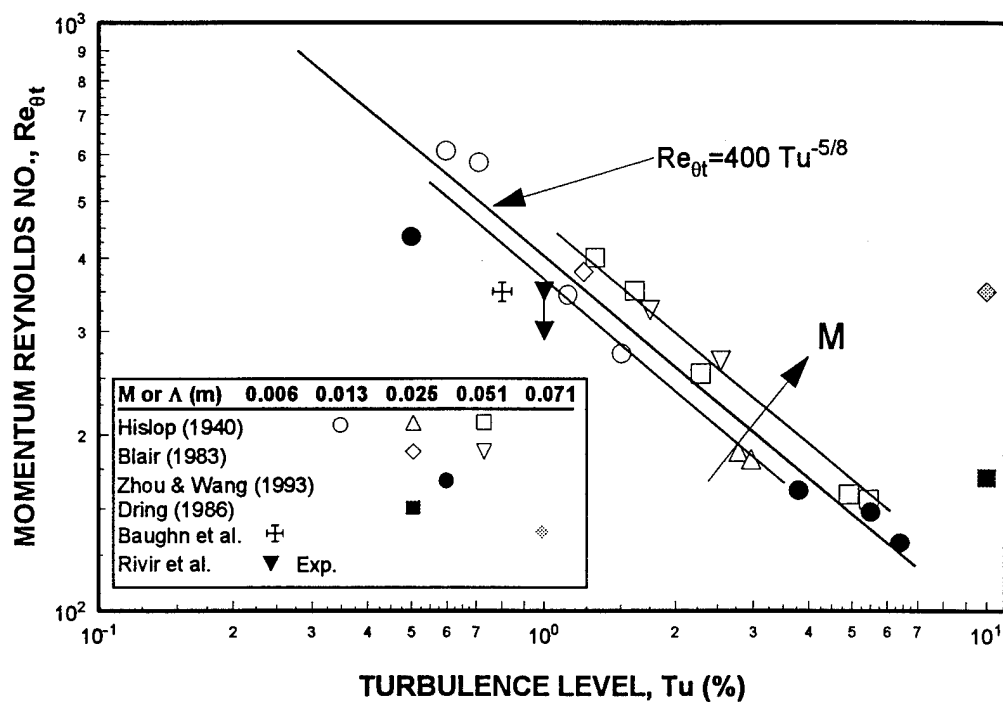


Figure 6. Momentum Thickness Reynolds Number at Transition

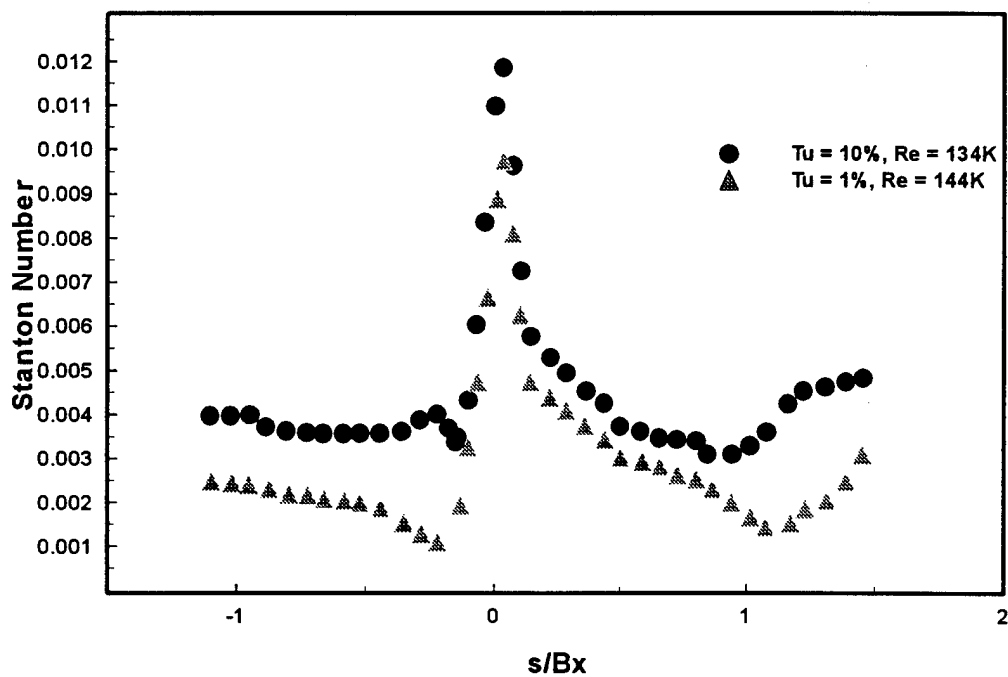


Figure 7. Dependence of Transition Length on Tu

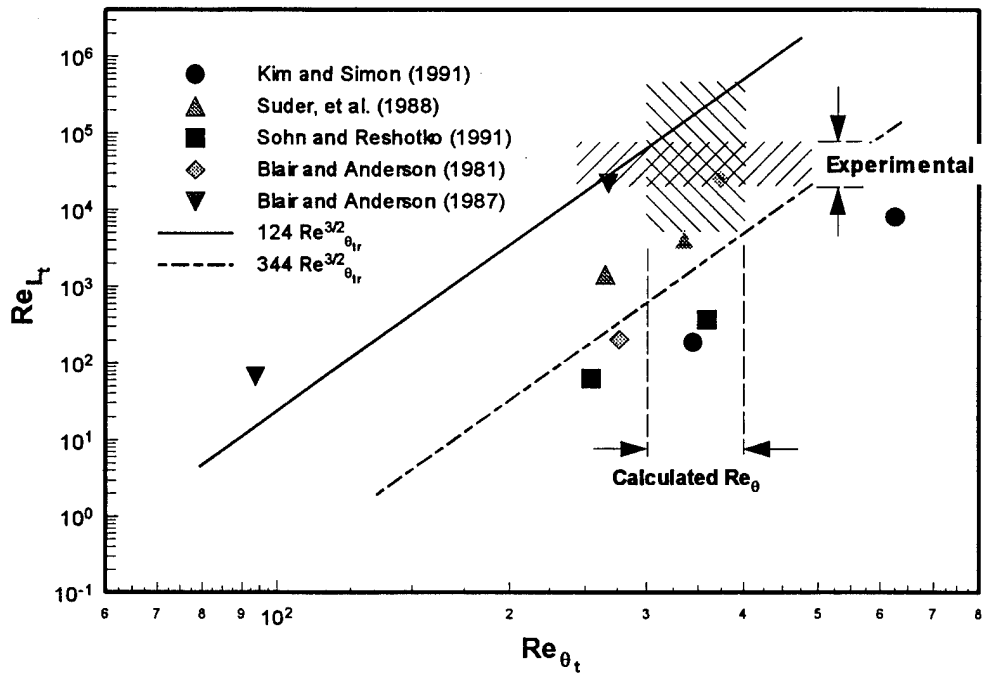


Figure 8. Transition Length Reynolds Number, 0 Pressure Gradient(124), Weak Pressure Gradient(344), (Simon,1994)

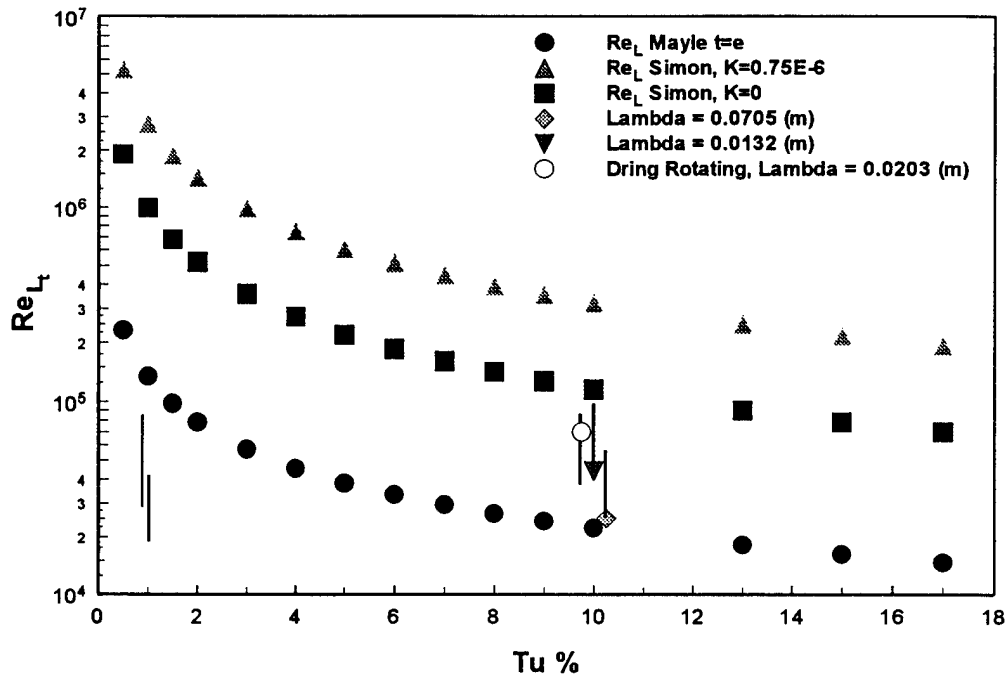


Figure 9. Comparison of Transition Length for 1% and 10% Tu Levels

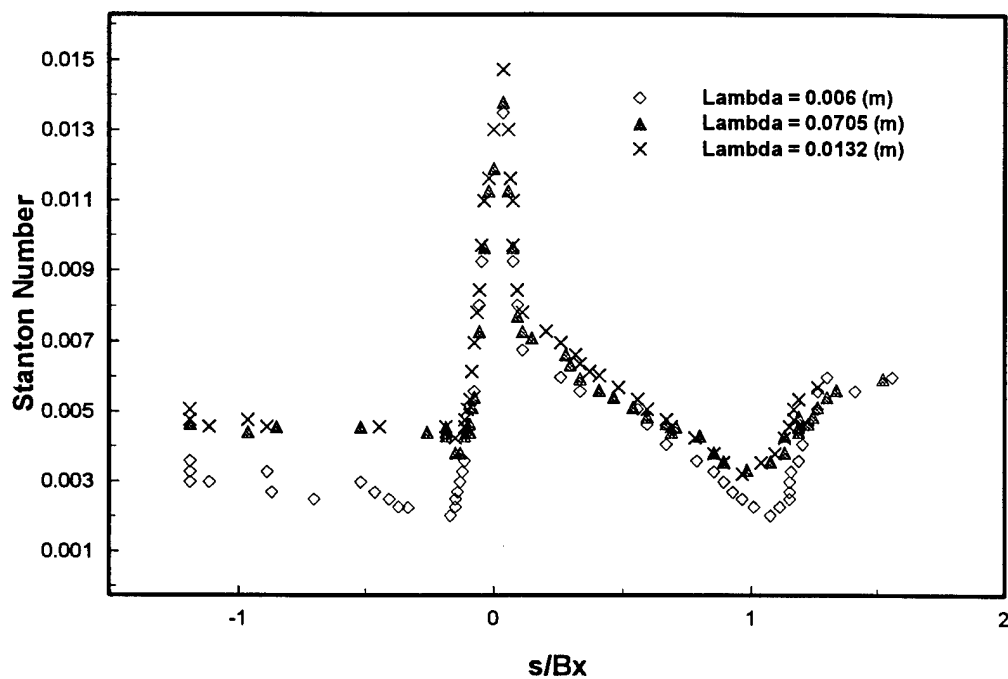


Figure 10. Liquid Crystal Measurements of Transition for Integral Scales 0.0705, 0.0132, (Tu 10%)
0.006 (Tu 0.5%)(Sharp and Harris, 1996)

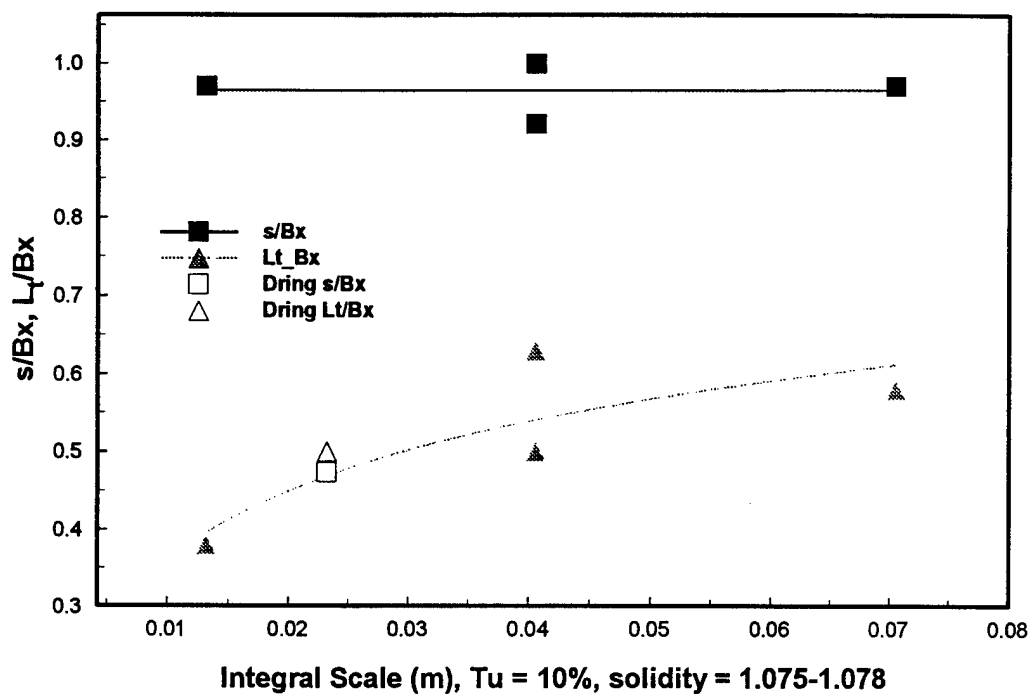


Figure 11. Transition Location and Length in % Projected Chord